# Plasma Opacities And High Precision Atomic Physics

LANL – EOS/Opacity V & V Workshop

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The Opacity Project Team: M. J. Seaton (UCL), et.al. : D. Mihalas (LANL), et.al.

## The OSU Team (www.astronomy.ohio-state.edu/~pradhan)

Sultana Nahar – Senior Research Scientist Graduate Students

- Guo-Xin Chen (Ex) PDF (Harvard ITAMP)
- Franck Delahaye (Opacities)
- Justin Oelgoetz (Also LANL)
- Maximiliano Montenegro
- Brian Larkins
- Rajni Tyagi

**Honorary Permanent Members** 

- Hong Lin Zhang (LANL)
- Werner Eissner (Stuttgart)

### Outline: Validity and Verification of EOS/Opacities

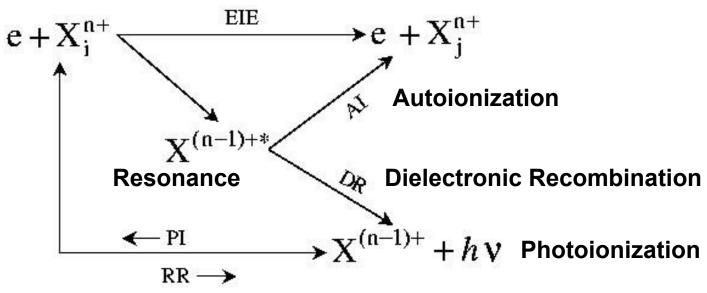
- "Academic" Perspective:
  - → Accuracy AND Completeness
- Astrophysical opacities (OP and OPAL)
  - → Current Problems: Radiative Accelerations
    New Solar abundances
- High Precision Atomic Physics
  - → Theory and Experiment
- Monochromatic X-ray opacities
- Nanoscience and Nanotechnology
  - → Biomedicine and Materials Research
- Plasma Fusion: ICF and Magnetic

### V &V – Academic Issues: Are we there yet?

- State-of-the-art atomic theory
- Continuous code development
- Study individual atomic processes in detail and compare with latest experiments (radiative transitions, photoionization, recombination, electron impact excitation)
- Large-scale calculations for laboratory and astrophysical opacities and spectral models
  - → The Opacity Project
  - → The Iron Project (Fe-peak elements)

## **Primary Atomic Processes in Plasmas**

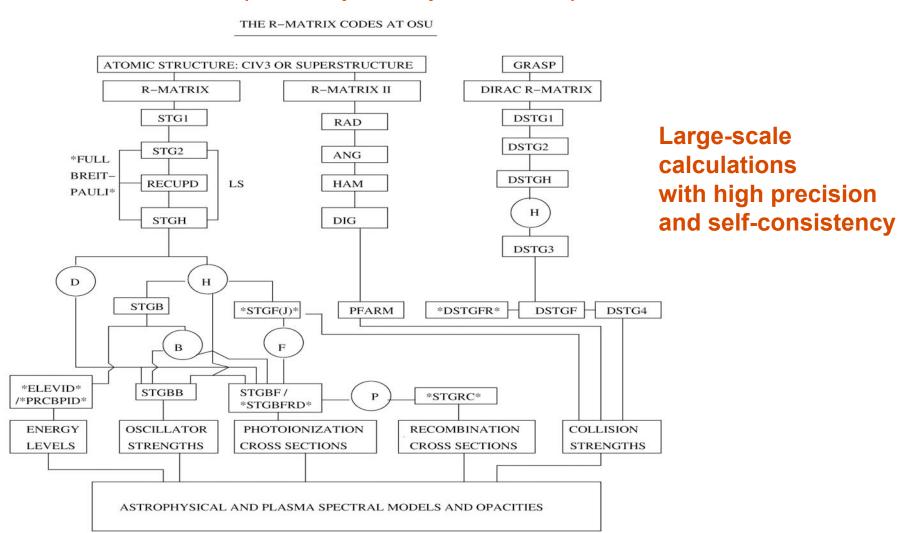
#### **Electron Impact Excitation**



**Radiative Recombination** 

The Coupled-Channel R-matrix method provides a self-consistent and unified treatment of all processes with one single wavefunction expansion

## Relativistic and Non-Relativistic R-matrix Codes For Atomic Processes (Ohio Supercomputer Center)



The Opacity Project: Two independent sets of opacity codes for V&V (i) M.J. Seaton, & Co., (ii) Yu, Mihalas, & Pradhan Only (i) employed for final OP tabulations

### The Opacity Project: 1983-2005

- Inception: 1983 → Group of > 30 researchers, 5 countries UK, US, France, Germany, Venezuela
- Cr, Mn, Ni Extrapolation + Kurucz
- First complete results 1994 → OP1
   (Seaton, Yu, Mihalas, Pradhan, MNRAS, 266, 805, 1994)
- OP1 results for stellar envelope opacities;
   did not include
  - → inner-shell processes
  - $\rightarrow$  stellar interior EOS for  $\rho > 0.01$  g/cc
- New OP work includes both
- On-line calculations for arbitrary composition
  - → <a href="http://www.osc.edu/hpc/opacities">http://www.osc.edu/hpc/opacities</a>
- CD-ROM from Anil Pradhan or Claude Zeippen

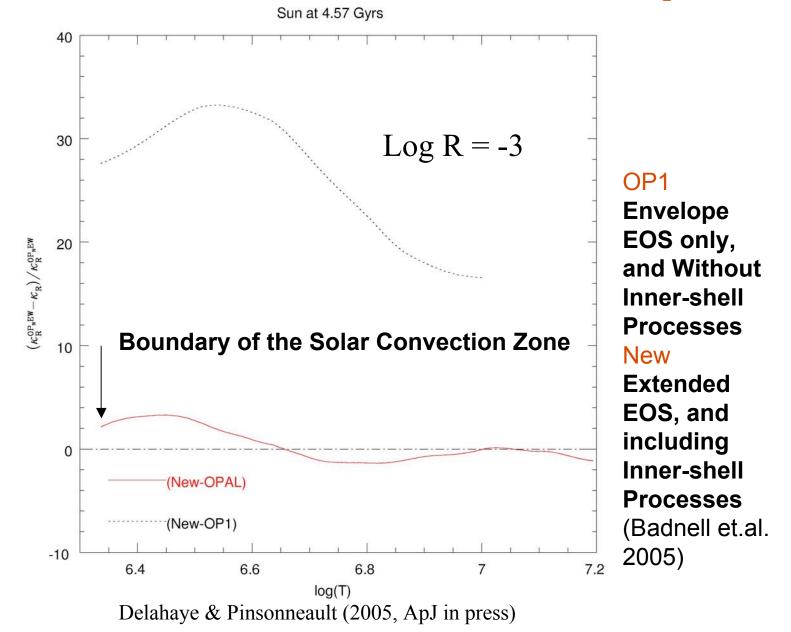
## Astrophysical Opacities: The Opacity Project (OP) and LLNL (OPAL)

- The OP work used a combination of R-matrix and atomic structure calculations for bound-bound and bound-free
- Mihalas-Hummer-Dappen (MHD) EOS
- New OP work uses "extended" MHD-EOS
  - → High-density uncertainties
  - Perturbed atom approximation
- Atomic data for inner-shell processes
  - → K-, L-, shell opacity

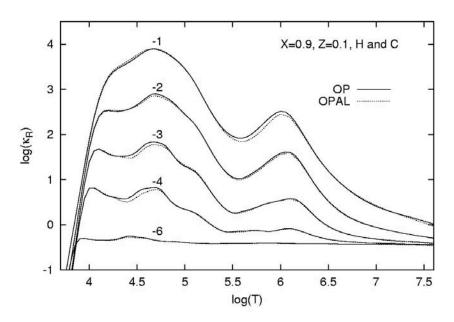
### Astrophysical Opacities – Validation and Verification

- New OP and OPAL agree in the MEAN opacities at the 5-10% level
- But radiative accelerations disagree by factors of 2-5!!
  - → Monochromatic opacity resolution
  - → Atomic physics accuracy
- V&V using Solar models similar in EOS, composition, central temperature, density, base of convection zone → very small differences

#### **OP vs. OPAL** → % **Differences in Rosseland Mean Opacities**



#### The Opacity Project (OP) and the OPAL Rosseland Mean Opacities



X=0.9, Z=0.1. H, C and Fe. C:Fe=2:1 OP -4 OPAL -----3  $\log(\kappa_{\rm R})$ 0 5.5 3.5 4 4.5 5 6 6.5 7 7.5 log(T)

Figure 5. Comparisons of  $\log(\kappa_R)$  from OP and OPAL for a H/C mixture with mass fractions X=0.9 for H and Z=0.1 for C. Curves are labelled by values of  $\log(R)$ .

Figure 10. Comparisons of  $\log(\kappa_R)$  from OP and OPAL for an iron-rich mixture: X = 0.9, Z = 0.1 and C:Fe=2:1 by number fraction. Curves are labelled by values of  $\log(R)$ .

(Log  $\kappa_R$  vs. Log T) at Log R =  $\rho / (T/10^6)^3$ 

#### RADIATIVE ACCELERATION

Given BB radiative flux F(r) at depth r in a star with  $T_{eff}$  and radius  $R_*$ , the radiative acceleration of element k is

$$g_{\tau ad}(r) = (\frac{1}{c})(\frac{M}{M_k})\kappa_R \gamma_k F(r), \qquad (1)$$

where  $\kappa_R$  is the Rosseland mean opacity at temperature T and density  $\rho$  at r, and  $\gamma_k$  is a dimensionless quantity representing the ratio of the momentum-transfer (mta) cross section to the total opacity cross section per atom

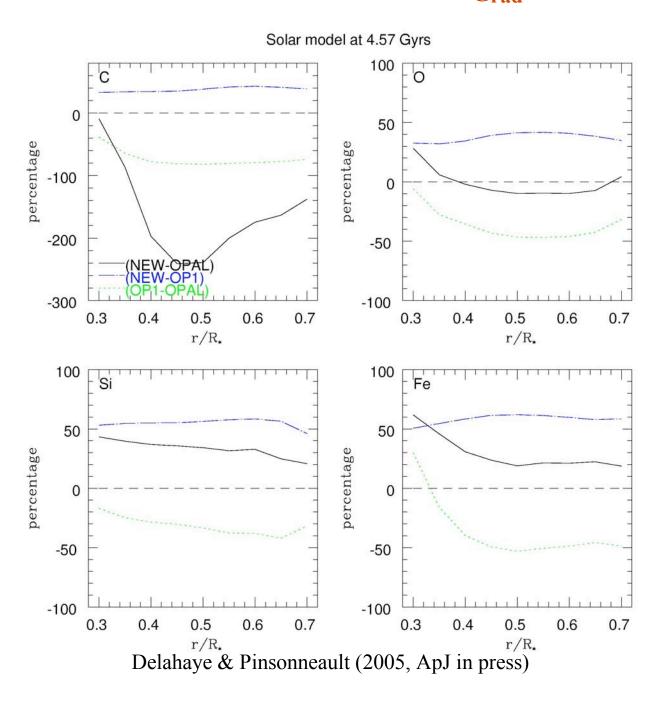
$$\gamma_k = \int \frac{\sigma_v^{mta}(k)}{\sigma_v(tot)} f_v d\nu, \qquad (2)$$

where

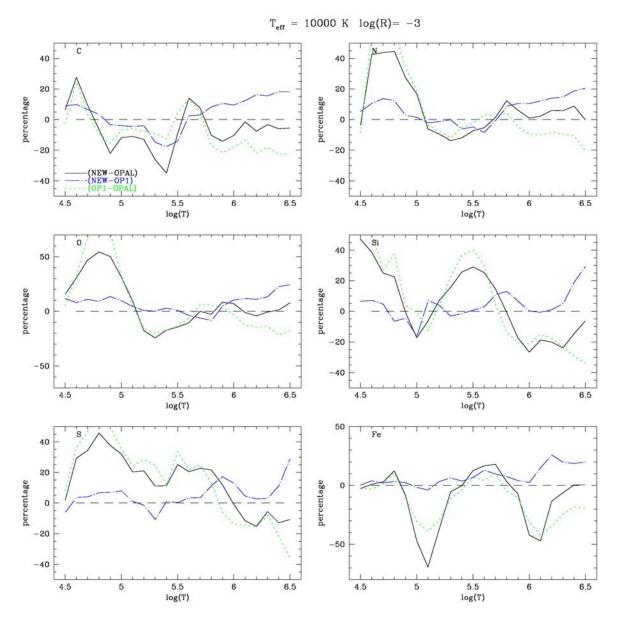
$$f_{\nu} = \frac{(dB_{\nu}/dT)}{(dB/dT)}.$$
 (3)

 $\gamma_{\kappa}$  is a measure of the specific opacity of element k relative to the total opacity, therefore much more sensitive to resolution and accuracy of atomic data than the Rosseland mean.

### OP vs. OPAL $\rightarrow$ % Differences in $g_{rad}$ for the Sun



#### **OP vs. OPAL** → % **Differences in Radiative Accelerations**



Delahaye & Pinsonneault (2005, ApJ in press)

### **New Solar Abundances (And Problems!)**

- Latest determination of solar abundances (Asplund et.al. 2005) – measurements and 3D hydro NLTE models – yield
  - → 30-40% lower abundances of C,N,O,Ne,Ar
- However, this disagrees with Helioseismology data (sound speed, BCZ, etc.), and
  - → would require the OP and OPAL opacities to be lower by about 10%; EOS has little effect (Bahcall et.al. 2004)

## Causes: Resolution

- Radiative acceleration  $g_{rad}$  or  $\gamma$  are more sensitive to resolution than the Rosseland mean opacities (RMO)
- Both OP and OPAL RMOs converge to 2% with 10<sup>4</sup> points, γ could differ by several factors depending on element and physical conditions
- OP data uses an adjustable mesh with better resolution

## Causes: Accuracy of Atomic Physics

- Only a relatively small subset of OP atomic data is from the R-matrix calculations
- Both OP and OPAL data may not differ much in absolute accuracy
- New Calculations Iron Project and Beyond
- Compare Close-Coupling R-matrix and other methods
- Verify results for fundamental atomic parameters for primary processes
- High precision atomic physics

### Coupled Channel R-Matrix Theory vs. Distorted Wave

#### **Coupled Channel Theory**

The wavefunction expansion,  $\Psi(E)$ , for a total spin and angular symmetry  $SL\pi$  or  $J\pi$ , of the (N+1) electron system is represented in terms of the target ion states as:

$$\Psi(E) = A \sum_{i} \chi_{i} \theta_{i} + \sum_{j} c_{j} \Phi_{j}, \qquad (1)$$

where  $\chi_i$  is the target ion wave function in a specific state  $S_iL_i\pi_i$  or level  $J_i\pi_i$ , and  $\theta_i$  is the wave function for the (N+1)th electron in a channel labeled as  $S_iL_i(J_i)\pi_i$   $k_i^2\ell_i(SL\pi)$   $[J\pi]$ ;  $k_i^2$  is the incident kinetic energy. In the second sum the  $\Phi_j$ 's are correlation wavefunctions of the (N+1) electron system.

- Ab initio treatment of important atomic processes with the same expansion: Eq.(1)
- Electron impact excitation, radiative transitions, and a self-consistent and unified treatment of photoionization and (e + ion) recombination, including radiative and dielectronic (RR+DR) (Nahar, Zhang, Pradhan)

All significant effects may be included

Infinite series of resonances are considered

## **Distorted Wave Theory Central Field Approximation**

- Includes only initial and final channels in Eq. (1); no summation
- Neglects channel coupling
- Resonance states (intermediate channels) NOT included in wavefunction expansion
- Resonances may be considered indirectly in the Isolated Resonance Approximation
- Finite number of resonances with n-extrapolation

## Accuracy AND Completeness: New Opacities Calculations

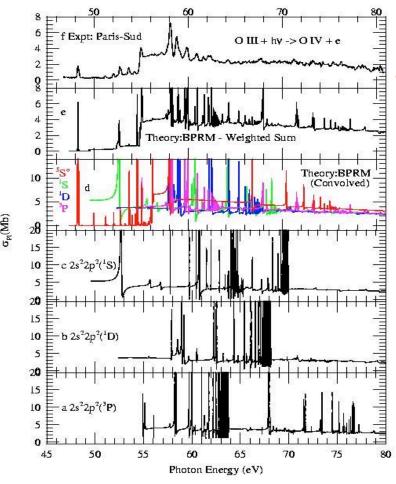
- Aim for high precision first, then completeness
- Benchmark state-of-the-art theoretical calculations with experiments for

Photoionization - Accelerator based Advanced Light Sources (Reno/Berkeley, Aarhus, Paris)

Recombination - Heavy ion storage rings (Heidelberg, Stockholm)

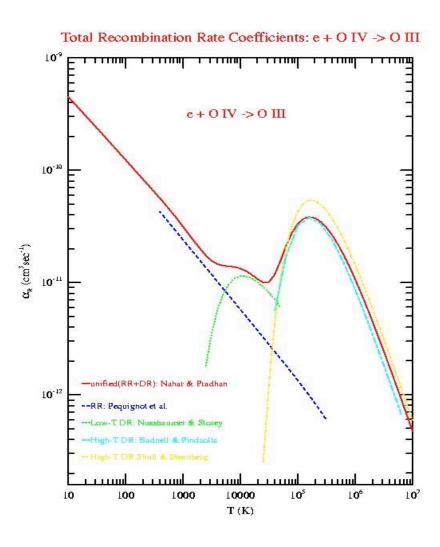
Electron-Ion Scattering - Electron Beam Ion Traps (Livermore, NIST)

## Photoionization of O III Comparison of R-Matrix Theory (Nahar 2003) and Experiment (Bijeau etal 2003)



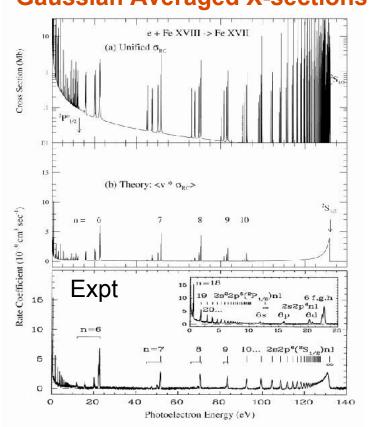
Experiment includes the ground state and metastable states of O III in the beam

## Unified (e+ion) Recombination Rate Coefficient (RR+DR)

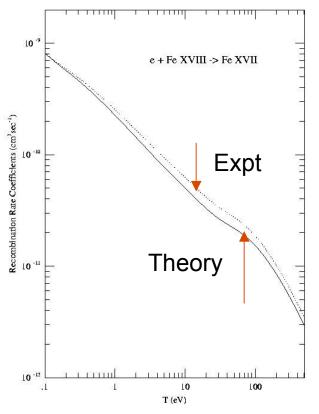


## Unified (e+ion) recombination: R-Matrix Theory and Experiments

#### **Gaussian Averaged X-sections**



#### **Maxwellian Averaged Rate**



Rates agree to < 20%

Theory: Pradhan, Nahar, and Zhang (ApJL, 549, L265, 2001)

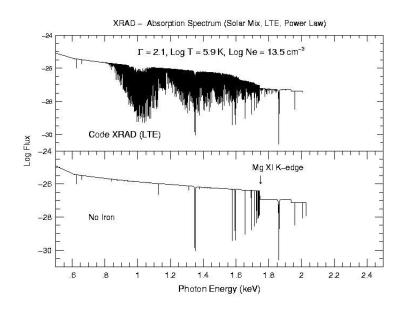
Expt: Savin et.al. (ApJS, 123, 687, 1999)

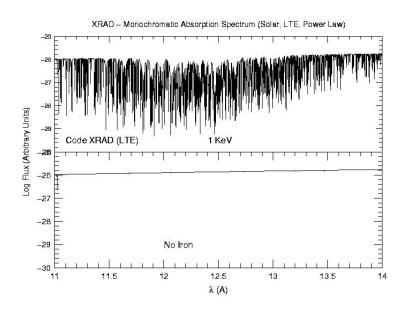
## Monochromatic Opacities

- Experimental verification of
  - → Cross sections and transition rates
  - → Monochromatic opacity/transmission spectra of elements
- Astrophysical verification with observed spectra

## Code XRAD – Theoretical X-ray Absorption Spectrum The Opacity Project and The Iron Project Data

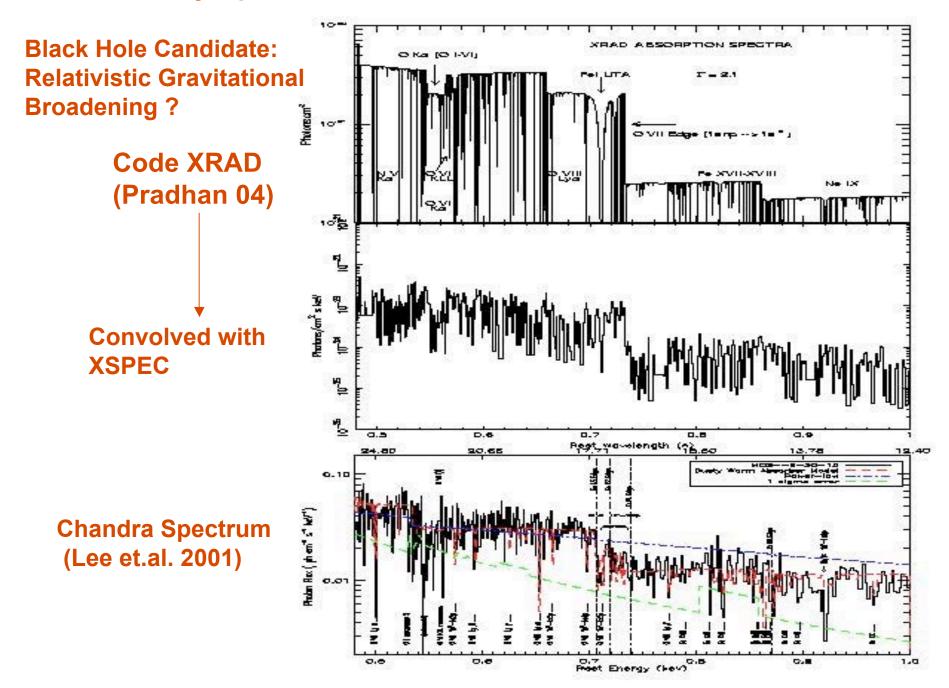
**(Pradhan 2004)** 





Power-law radiation field (NOT Blackbody), Monochromatic opacities and spectrum for arbitrary mixtures

#### Mono X-ray Opacities: Modeling The Spectrum of AGN MCG-6-30-15

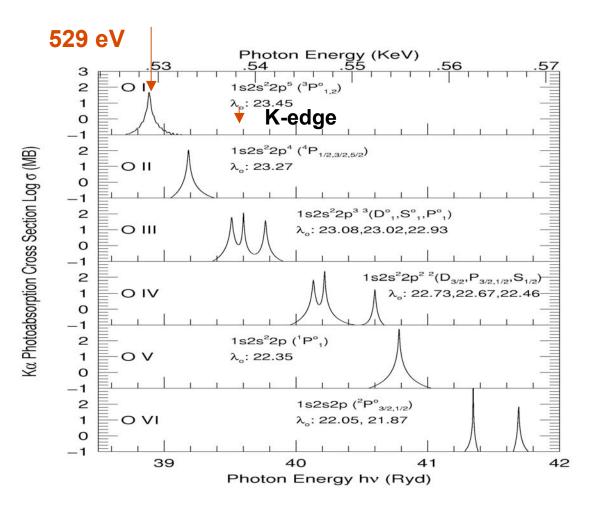


### NANOSPECIROSCOPY

## Computational Nanoscience at Fundamental Atomic and Molecular Scales (OSU)

- Nanobiomedicine and Nanomaterials
- Broadband (indiscrimate!) imaging yields pictures, but not detailed nanoscopic information
- Spectroscopy is the most powerful tool "A spectrum is worth a thousand pictures"
- Paradigm shift from imaging to spectroscopy, such as occurred in astronomy
- Spectroscopy should be far more efficient with reduced radiation exposure by targeting spectral features in atoms and molecules

## Resonance Peaks in X-Ray Photoabsorption By Oxygen



Resonance in neutral O at 0.529keV; X-ray absorption cross section is higher by factor of up to 100 than at other energies

AVOID X-RAYS AT 529 eV → ~ 100 TIMES MORE DAMAGE TO HUMAN BODY !!

Pradhan, Nahar, Delahaye, Chen, Oelgoetz (2003)

### Spectral 'Windows' in X-ray opacities

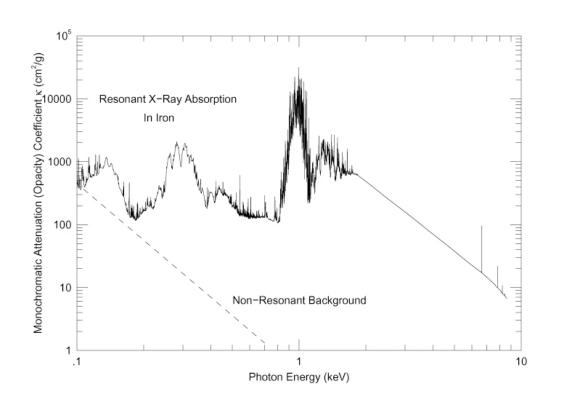
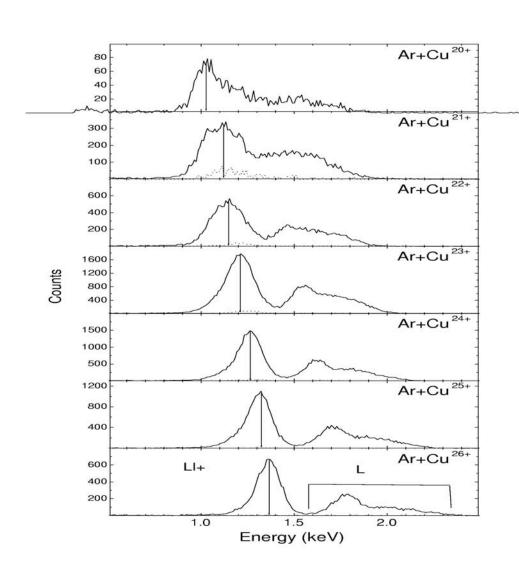


Fig. 1. The enhancement in X-ray photo-absorption in iron due to low energy resonance complexes. Compared to the nonresonant background, the attenuation coefficients may be up to several orders of magnitude higher, particularly in specific 'spectral windows' such as the one at 1 KeV due to L-shell excitations. Heavier elements will have such features at much higher energies.

Lighter 'biogenic' elements (H,C,N,O) have far lower absorption coefficient at high energies; beyond the K-edge, cross section ~ E-3.

X-rays are absorbed by iron and heavier elements with orders of magnitude higher efficiency at energies of resonance-arrays.

## **Experiment: X-Ray Fluorescent Emission** "Spectral Windows" From Copper



Preliminary results from collaborators using the Pelletron: Heavy ion Accelerator at the Tata Institute For Fundamental Research, Mumbai, India (A. Kumar & L. Tribedi, private communication)

More experiments needed to locate peak emission windows

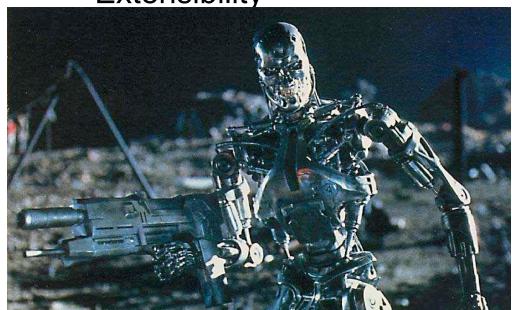
## Conclusion

- Definitive opacities with state-of-the-art atomic physics have not yet been computed (EOS?)
- Calculations are needed for heavy elements, Iron and beyond, including relativisitic effects using Breit-Pauli or Dirac R-matrix codes
- Collaboration with LANL, LLNL might be desirable to compare detailed opacities
- Nanotechnology, fusion, and other applications next generation of AM codes

## New Computational Technology For Atomic and Molecular Physics

- Tensor Contraction Engine (TCE) for automatic formula derivations and parallel implementation of any given model of wave function theory.
  - Expediency
  - Optimization & Parallelization
  - Maintainability & portability

Extensibility



"It doesn't feel pity, or remorse, or fear."

The Terminator

(And has no sense of humor)